

Mean and Median of RVs

- For each PDF, calculate the mean and the median:
 - $f(x) = x^{-2}$ for $\frac{1}{2} \leq x \leq 1$ and $f(x) = 0$ otherwise.
 - $f(x) = x(3x^2 + \frac{1}{2})$ for $0 < x \leq 1$ and $f(x) = 0$ otherwise.
 - $f(x) = c(1 - x^2)$ for $-1 < x < 1$ and $f(x) = 0$ otherwise.
- Chromosomal recombination** is a process by which two chromosomes join together and exchange DNA. The point along the DNA at which the join occurs is randomly located. Suppose X is a **discrete** RV denoting the location with $0 \leq X \leq 2$. In an experiment, $E[X] = 1$ and $Var[X] = \frac{2}{3}$. Are the findings consistent with the hypothesis that all locations along the chromosome are uniformly likely? Explain.

Midterm 2 Review

- Find a, b or c given the PDF, then find the CDF.
 - $f(x) = c(1 - x^2)$ for $-1 < x < 1$ and $f(x) = 0$ otherwise.
 - $f(x) = c/x^2$ for $x > 10$ and $f(x) = 0$ otherwise.
 - $f(x) = a + bx^2$ for $0 \leq x \leq 1$ and $f(x) = 0$ otherwise, given $E(X) = \frac{3}{5}$.
- Suppose you take a random sample of 10 tickets without replacement from a box containing 20 red tickets and 30 blue tickets.
 - What is the chance of getting exactly 4 red tickets?
 - Repeat (a) for sampling with replacement.
- Suppose that we observed 10 frogs in a pond during the observation period of 100 days. Find the Poisson approximation to the probability of observing $X = k$ frogs each day. Using that approximation to calculate the probability that
 - you observe precisely one frog today?
 - you observe more than one frog today?
 - you observe no frogs today?
- Suppose that a test for opium use has a 2% false positive rate and a 5% false negative rate. That is, 2% of people who do not use opium test positive for opium, and 5% of opium users test negative for opium. Furthermore, suppose that 1% of people actually use opium.
 - Find the probability that someone who tests negative for opium use does not use opium.
 - Find the probability that someone who tests positive for opium use actually uses opium.

Source: some from Stewart's *Biocalculus*, the others from internet.